Platonic Solids are solids whose faces are
congruent regular polygons. The same number of faces meet at each vertex of the Platonic Solid.

TETRAHEDRON
$E=6, V=4, F=4$

CUBE
$\mathrm{E}=12, \mathrm{~V}=8, \mathrm{~F}=6$
The sum of the angles at the centre is $360^{\circ}$. So the centre lies flat on the ground.


OCTAHEDRON $\mathrm{E}=12, \mathrm{~V}=6, \mathrm{~F}=8$


The sum of the angles at the centre is less than $360^{\circ}$. So the corner of a solid can be formed.


The sum of the plane angles meeting at a vertex should be less than $360^{\circ}$ to form a solid. This implies that only five Platonic Solids are possible, as the table below shows.


| No. of faces meeting at Type a vertex of face | 3 | 4 | 5 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Equilateral triangle $\mathrm{N}=3$ Angle $=60^{\circ}$ | $\text { sum }=180^{\circ}$ <br> (Tetrahedron) | $\text { sum }=240^{\circ}$ <br> (Octahedron) | $\begin{aligned} & \text { sum }=300^{\circ} \\ & \text { (Icosahedron) } \end{aligned}$ | sum $=360^{\circ}$ | sum $=420^{\circ}$ |
| $\begin{aligned} & \text { Square } \\ & \mathrm{N}=4 \\ & \text { Angle }=90^{\circ} \end{aligned}$ | $\begin{aligned} & \text { sum }=270^{\circ} \\ & \text { (Cube) } \end{aligned}$ | sum $=360^{\circ}$ | sum $=450^{\circ}$ | sum $=540^{\circ}$ | sum $=630^{\circ}$ |
| $\begin{aligned} & \text { Pentagon } \\ & \mathrm{N}=5 \\ & \text { Angle }=108^{\circ} \end{aligned}$ | $\text { sum }=324^{\circ}$ <br> (Dodecahedron) | sum $=432^{\circ}$ | sum $=540^{\circ}$ | sum $=648^{\circ}$ | sum $=756^{\circ}$ |
| Hexagon $N=6$ <br> Angle $=120^{\circ}$ | sum $=360^{\circ}$ | sum $=480^{\circ}$ | sum $=600^{\circ}$ | sum $=720^{\circ}$ | sum $=840^{\circ}$ |

